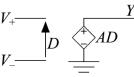


Operational amplifier is one of the most common electronic building blocks used by engineers. It has two input terminals: V⁺ and V⁻, and one output terminal Y. It provides a gain A, which is usually very high – around 100,000 x at low frequency. It has very high input impedance – > $10M\Omega$. It has a low output impedance. In other words, op-amp behaves almost like an ideal amplifier.

We can model an op amp as shown here:

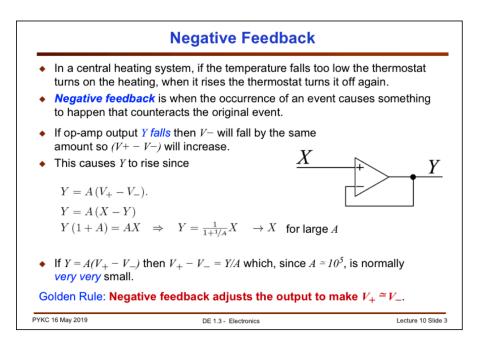


D is the voltage difference = $(V^+ - V^-)$.

The output Y is D x A, where A is the gain. Since A is very large, D is generally very small. For example, if the output voltage Y is +5V, A is 10^5 , D is only $50\mu V$. The scope you have been using in the laboratory cannot even measure down to this voltage level!

An op-amp is actually very complex inside. However, as a user of op amp, and if you use it properly, you can simply ignore its internal complexity and treat it more or less like a perfect differential amplifier (i.e amplifying the difference voltage).

Opamps belong to a type of electronic components known as integrated circuits (ICs). The packaging is as shown here where pin 1 is always on the left of the notch in the package and/or indicated with a dot.



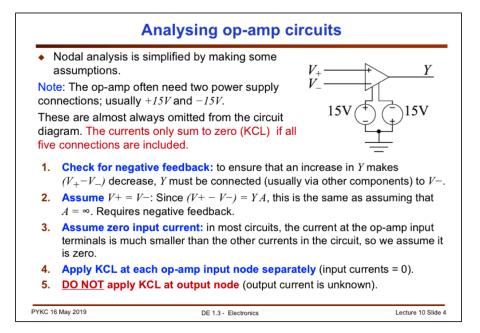
Before we consider how to build an amplifier with an op-amp, let us consider the concept of **negative feedback**. Simply put, when an event causes something to change, the change itself will counteract the original event.

Shown here is the op-amp using negative feedback. The output Y is connect to the V₋ input of the op amp. If output Y falls (the event), it will cause V₋ to fall (the change). However, V₋ falling will increase the difference voltage (V₊ - V₋). This causes Y to rise, thus counteracting the initial fall in Y.

The calculation shown here demonstrate that provided A is large,

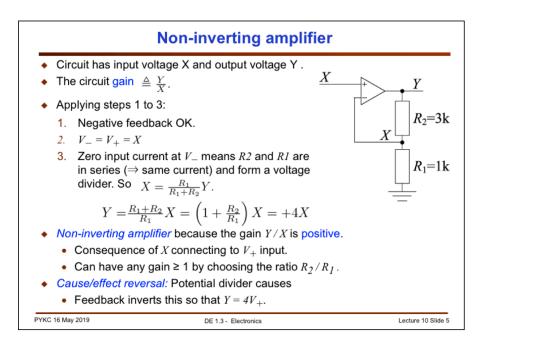
Y = X. Connecting Y to the $V_{\scriptscriptstyle -}$ input ensure that this is always true with this circuit.

Note the golden rule: by feeding the output back to the NEGATIVE input of the op-amp which has very large gain, the circuit makes sure that $(V_+ - V_-)$ approaches zero!



Opamp requires power supply for it to work. For the sake of simplicity, we assume that the op-amp uses dual voltage supply with a +ve and a -ve voltage source as shown here. We will relax this assumption later.

To conduct analysis on opamp circuits, we have to make some assumptions as shown here.



Shown here is one of the most commonly used op-amp circuit to provide non-inverting amplification.

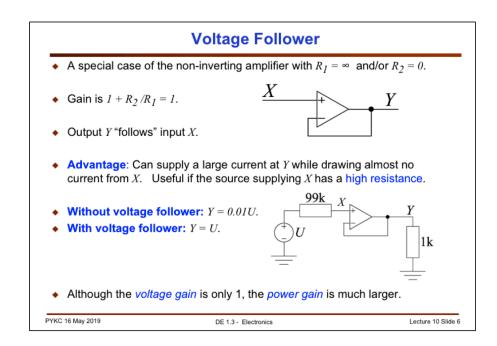
We check through the steps considered in the previous slide. This circuit has negative feedback. Input voltage X is connected to V_+ . Therefore the voltage at V_- is also X.

Input current is zero. Therefore X is the voltage divider of Y as shown here.

For such non-inverting op-amp circuit, Gain is always given by:

$$Gain = \frac{Y}{X} = (1 + \frac{R_2}{R_1})$$

For the circuit shown here, the gain is +4.



There is a special case for the non-inverting op-amp circuit. If you make R2 = 0, and remove R1, then the gain is 1. In fact even if R2 is larger than zero (say 1k), the ratio R2/R1 is still zero since R1 is infinite.

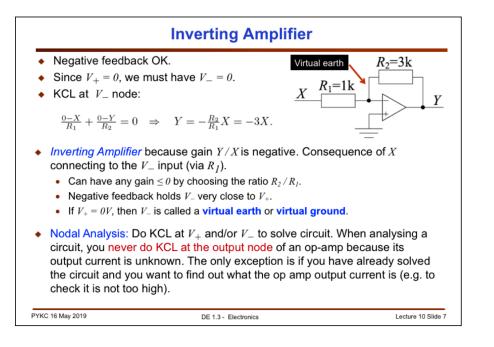
This circuit is known as voltage follower, or voltage buffer – output Y always follow input X.

This circuit may first appear pointless – Y is the same as X, why not just use X in the first place?

The reason why this circuit is useful is because it **ISOLATES** the output from the input by presenting a high impedance to the source (Rin is high) and low impedance to the load, hence behaving like an ideal amplifier, but with gain of 1.

Let us consider the example here. The source voltage U has a resistance of $99k\Omega$. If we connect this directly to a 1Ω load, the output Y = 0.01U (voltage divider principle). The drop of voltage is due to the loading effect of the 1k resistor on the source.

When you put the voltage follow between U and the 1k load resistor, the source U sees the very high input impedance of the op-amp (>10M Ω), therefore the input X is effective U. The output resistance of the op amp is low. The negative feedback also helps. If the loading effect of the 1k resistor causes Y to drop, this will cause V- input to drop, and raising Y, thus correcting the loading effect.

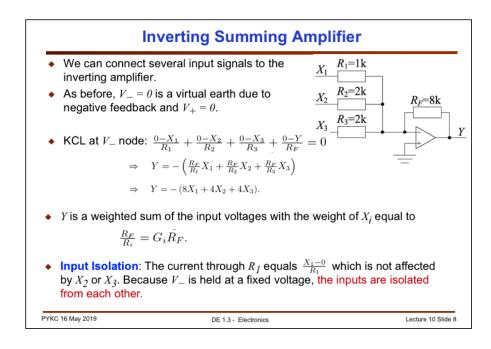


This is the circuit for an inverting amplifier using an op-amp. Applying KCL at the V_{-} node gives the following equation:

$$Gain = \frac{Y}{X} = -\left(\frac{R_2}{R_1}\right)$$

Since the V₋ node is at the same voltage potential of the V₊ node, which is ground (or earthed), we call V₋ node in this circuit the virtual earth or virtual ground.

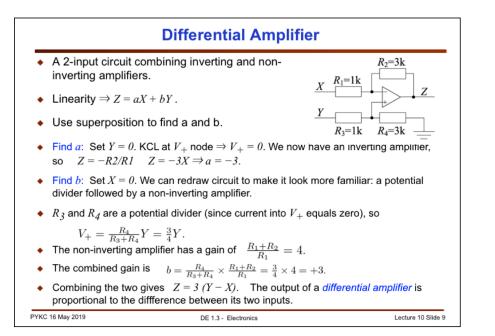
Unlike the non-inverting amplifier case, which MUST have a gain ≥ 1 , inverting amplifier like this can have any gain, larger or smaller than 1.



With inverting amplifier, since the V- node is virtually zero, you can connect multiple sources to this node via a resistor and produce a summing amplifier.

Apply KCL at V- node and you see the summing effect immediately. Each voltage is weighted by the ratio of the feedback resistor $R_{\rm F}$ and the feeding resistor $R_{\rm i}$ (i.e. the weighting is - $R_{\rm F}/R_{\rm i}$).

The fact that the V- node is held at a fixed voltage (in this case 0v, but it could have been a different voltage, as we will see later), the effect of input sources X1, X2 etc is isolated from each other.



We can combine the structure of the inverting AND non-inverting amplifier together to form this differential amplifier. The best way to understand this is to apply the principle of superposition.

Consider the effect of X on output Z with Y set to zero. The output due to X alone is: $Z_{Y} = -\frac{R_2}{2}X$

$$Z_X = -\frac{2}{R_1}$$

Consider the effect of Y on output Z with X set to zero. The output due to Y alone is more complicated. Firstly, Y is reduced by the voltage divider before reaching the V+ input.

$$V_{+} = \frac{R_4}{R_3 + R_4} Y$$

This is amplified according to the non-inverting amplifier gain:

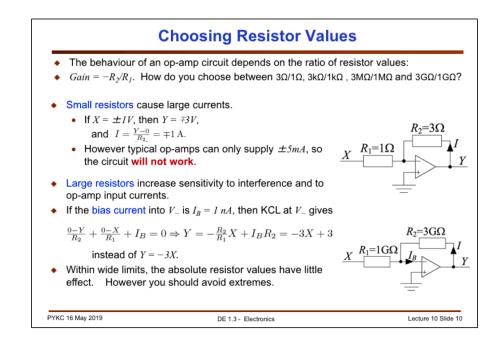
$$Z_Y = (1 + \frac{R_2}{R_1}) \times (\frac{R_4}{R_3 + R_4})Y$$

Now assume that $R_2 = R_4 = 3k$, and $R_1 = R_3 = 1k$.

$$Z_Y = (1 + \frac{R_2}{R_1}) \times (\frac{R_2}{R_1 + R_2}) Y = \frac{R_2}{R_1} Y$$

Therefore

$$Z = Z_X + Z_Y = (\frac{R_2}{R_1}) \times (Y - X) = 3 \times (Y - X)$$



So far, we assume that the op-amp behaves like an ideal amplifier with infinite gain A, infinite input resistance Ri, and zero output impedance R_0 .

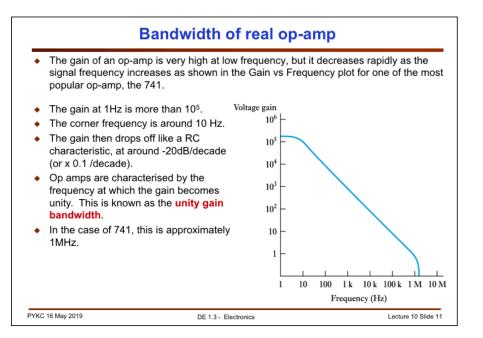
These assumptions only hold if the resistors we use to construct the circuit are sensible. So how do we choose these resistor values?

If we use too low a resistor value, the output current required is too much – no good.

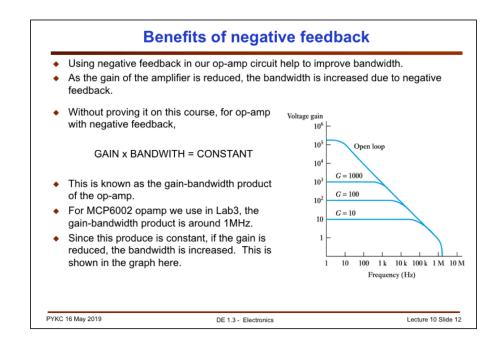
If we use too high a resistor value, the input current into the opamp is no longer negligible. Then the gain equation we derived using KCL at the input node is no longer valid.

In general, we use resistor values in $k\Omega$ to $100k\Omega$ region.

In the next slide, we will consider the assumption of infinite gain A.



For a practical op-amp, the gain is only very high at low frequency. Shown here is the Gain vs Frequency characteristic of a 741 opamp, one of the most popular op-amp in the history of electronics. The gain is over 100,000 at frequency below 10Hz. However, the characteristic is similar to the of an RC low pass filter. The corner frequency is only 10Hz. It then falls off at -20dB (or x 0.1) / decade. The gain at 1MHz becomes around 1 (i.e. it stop behaving as an amplifier).



The detail analysis of the impact of this falling gain on bandwidth when we use negative feedback is beyond the scope of this module. However, it is worth stating the following observation:

Due to negative feedback, the produce of the overall circuit gain and the effective bandwidth (i.e maximum frequency for this to behave like an amplifier) is a constant. This product:

Gain x Bandwidth = gain-bandwidth product = constant.

For MCP6002, the product is around 1MHz, or 10⁶.

The result of this is shown in the plot here.

